

Name:

**Math 10a**  
October 23, 2014  
Quiz #6

1. (2 points) Write down, in summation notation, the estimate for

$$\int_{-1}^1 \frac{1}{\sqrt{2\pi}} e^{-x^2/2} dx$$

using a left Riemann sum with 100 intervals.

2. (3 points) If you were to estimate the area under the graph of  $\sin(x)$  from 0 to  $\pi$  using the trapezoid rule, how many trapezoids would you need to guarantee accuracy to within  $1/10$ ? You may use:

$$\text{error}(T_n) \leq \frac{(\max |f''|)(b-a)^3}{12n^2}$$

and the fact that  $\pi^3 = 31.00627\dots$

3. Consider  $f(x) = x^2 - x$

(a) (1 point) Sketch the graph of  $f$  from  $x = -1$  to  $x = 1$ .

(b) (1 point) Draw the five rectangles of width  $2/5$  which approximate the area under the curve using the midpoint rule.

(c) (3 points) Approximate

$$\int_{-1}^1 (x - x^2) dx$$

using a midpoint rule with five intervals. Simplify your answer to a single fraction.